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Charged Lepton Flavour Violation

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Charged lepton flavour violating processes are naturally present in many extensions of the Standard Model. After a brief overview on the experimental situation, an effective-field-theory framework is described that allows to interpret and compare the various experiments in a consistent way.

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1. Introduction

In the Standard Model (SM) without right-handed neutrinos, lepton flavour is conserved. This is an accidental symmetry simply due to the fact that it is not possible to write down a renormalizable and gauge-invariant operator that violates (charged) lepton flavour. In the quark sector the situation is different. Since all quarks have non-vanishing (and different) masses, the distinction between mass eigenstates and interaction eigenstates leads to “quark flavour violation”.

If we take into account neutrino masses, lepton flavour is also violated. It is true that taken alone, this violation is very weak in the sense that it leads to branching ratios for charged lepton flavour violating (cLFV) decays that are unobservable in any conceivable experiment. However, the crucial message is that as for quark flavour, there is nothing sacred about lepton flavour conservation.

As a consequence, beyond the Standard Model (BSM) physics will lead to cLFV unless special care is taken to prevent it. The fact that we have not seen it yet despite substantial experimental effort has two possible explanations: either BSM has some mechanism to prevent cLFV, or the new physics (NP) scale related to cLFV is so high that the corresponding interactions are extremely suppressed at the low-energy scale of the experiments. The first option is actually a step back from the SM. While the absence of observable cLFV has a natural explanation within the SM, going beyond invalidates this and leads to a problem that was not present in the SM. Creating new problems is not what we usually expect from BSM physics. The second option is much more natural, albeit somewhat sobering. Taken at face value, it leads to the expectation of NP at an extremely high scale (at or above 10^{10} GeV). If this was the case, neutrino masses would be *the* NP we observe and cLFV is the next best chance, but direct searches at the high-energy frontier are bound to fail. The only consolation in this scenario is that there is no reason for there to be only a single scale of NP. Indeed, currently the *B*-anomalies for example offer a fragile glimmer of hope that other NP is present at much smaller scales (see e.g. [1]).

In either case, the investigation of cLFV processes offers the possibility to test the SM to very high scales or actually find BSM. Since this will be indirect evidence, it is crucial to consider as many observables as possible. Indirect evidence from a single observable will at most tell us “there is something”, but never give enough information to conclude what it is. A comprehensive study of cLFV however will be able to seriously constrain the infinitely many options of BSM and, in the best of worlds, point us to the option nature has chosen.

2. Observables

There is a plethora of processes where we can look for cLFV effects. The most stringent limits have been obtained for the golden muon decay channels, namely $\text{Br}(\mu \rightarrow e\gamma) < 4.2 \times 10^{-13}$ [2], $\text{Br}(\mu \rightarrow 3e) < 1.0 \times 10^{-12}$ [3] and muon conversion in the field of a nucleus. As an example of the latter, for muon conversion in a gold atom the limit is $\text{Br}_{\mu \rightarrow e}^{\text{Au}} < 7 \times 10^{-13}$ [4], where the decay rate is normalized by the capture rate. As I will argue below, the limits on these observables are highly complementary and improving the limits on all of these observables will provide important information. Luckily, the near future will see a lot of experimental progress. MEG II will improve the limit on $\mu \rightarrow e\gamma$ by an order of magnitude [5], while Mu3e will increase the significance on

$\mu \rightarrow 3e$ by several orders of magnitude [6]. For muon conversion, COMET [7] and Mu2e [8] will also improve the sensitivity by about four orders of magnitude, using aluminium.

Given that the SM rate for these processes are tiny it is often said that these searches are background free. However, there is of course background from 'boring' SM processes. Apart from the reducible (accidental) background, which can be tackled by improving the resolution of the detectors, there is the irreducible background. For $\mu \rightarrow e\gamma$ and $\mu \rightarrow 3e$ this is due to SM processes $\mu \rightarrow e\gamma\nu\bar{\nu}$ and $\mu \rightarrow 3e\nu\bar{\nu}$ in the region where the neutrinos have very little energy. These processes have by now all been calculated at NLO in the electromagnetic coupling, providing reliable predictions to estimate the number of irreducible background events [9, 10, 11, 12, 13]. For muon conversion, an irreducible background appears through the decay of the muon in orbit. Since this decay happens in the field of the nucleus, the energy distribution of the emitted electron has a tail up to the muon mass (minus binding energy). Again, there exist reliable theoretical predictions for this decay [14]. For all cases the bottom line is that the irreducible background is not preventing measurements with the proposed sensitivity.

Apart from muon decays, also tau decays offer a very rich field to study cLFV. Typically, the experimental constraints are weaker by several orders of magnitude. For example, the limits on the various branching ratios for $\tau \rightarrow 3\ell$ with $\ell \in \{e, \mu\}$ are all about $\text{Br}(\tau \rightarrow 3\ell) \lesssim 2 \times 10^{-8}$ [15] and the limits for $\tau \rightarrow \ell\gamma$ are roughly $\text{Br}(\tau \rightarrow \ell\gamma) \lesssim 4 \times 10^{-8}$ [16, 17]. However, in the case of the τ there are numerous further LFV decays possible and many have strong experimental constraints. To mention but a few, we have e.g. $\text{Br}(\tau \rightarrow \ell\pi^0) \lesssim 1 \times 10^{-7}$ [18, 19], $\text{Br}(\tau \rightarrow \ell K_S^0) \lesssim 3 \times 10^{-8}$ [20, 21] and $\text{Br}(\tau \rightarrow \ell K^+ K^-) \lesssim 4 \times 10^{-8}$ [22]. Once Belle II is in operation, many of these branching ratios will be scrutinized even more stringently. Should there ever be evidence for NP in one of these channels the presence of similar observables will be very beneficial to assess the reliability of the evidence as well as constraining possible BSM explanations.

3. Looking for BSM

The main motivation to investigate cLFV is to constrain the SM and look for BSM. Since cLFV will only give indirect information it is necessary to compare the information on the branching ratios to a hypothesis. Ultimately, of course we want to find the ultraviolet (UV) complete theory that describes BSM physics and compare its predictions to cLFV data. Unfortunately, choosing the appropriate UV complete theory requires divine inspiration, resulting in very specific case by case studies in this approach.

In order to be more general, it is possible to consider so-called simplified models. Without worrying about UV completion new particles (typically scalars or vectors) are introduced. The degrees of freedom then are the mass of the new particle and its couplings to SM particles and constraints on these parameters are obtained through cLFV data.

Making the approach even more general we can work with effective theories. In this case no new dynamical degrees of freedom are introduced at all and the effects of BSM physics are encoded in Wilson coefficients of higher-dimensional operators. The latter are constructed from SM fields, ensuring gauge and Lorentz invariance.

In practice, the most promising approach is probably bottom up, i.e. starting from an effective theory. Once a pattern of deviations in Wilson coefficients is established, a simplified model that

produces these coefficients can be looked for. In case such a simplified model can be found, its embedding in a UV complete theory would be the final step. In fact, currently precisely such a programme has been started in the context of B anomalies.

In the reminder we will focus on an effective field theory (EFT) approach. The standard expectation of BSM physics is that it is related to new heavy degrees of freedom at a scale Λ , considerably above the electroweak (EW) scale $\Lambda \gg M_{ew}$. On the other hand we are using experiments at much smaller scales $\{m_\mu, m_\tau\} \ll M_{ew} \ll \Lambda$. Thus, it is very natural to use an effective theory where the (unknown) heavy degrees of freedom have been integrated out. After all, EFT are precisely made for situations with two (or more) widely different scales. In fact, we have to use two different EFT. Integrating out NP at the scale Λ will lead to a tower of higher-dimensional operators which respect the gauge symmetries of the SM, $SU_c(3) \times SU_L(2) \times U_Y(1)$. This EFT is called SMEFT. However, for muon and tau decays, also the degrees of freedom with EW scale can (and should) be integrated out. Below the EW scale, the symmetry of the theory is $SU_c(3) \times U_{em}(1)$, and to be completely general, all (Lorentz invariant) operators respecting this symmetry should be included. Of course, in B physics, such an effective theory has been used for decades. In the context of cLFV, we will refer to it as LEFT (low energy EFT).

In what follows, we will consider these two EFT and how they are related to observables in some more details.

4. Effective theory above the electroweak scale

The Lagrangian of SMEFT has a single operator of dimension five [23], related to neutrino masses. Including also dimension 6 operators [24] we write

$$\mathcal{L}_{SMEFT} = \mathcal{L}_{SM} + \frac{1}{\Lambda} C^{(5)} Q^{(5)} + \frac{1}{\Lambda^2} \sum C_i^{(6)} Q_i^{(6)} + \dots \quad (4.1)$$

The Wilson coefficients at the high scale, $C_i^{(6)}(\Lambda)$, directly encode the information of the BSM theory and can be considered as a parameterization of our ignorance. However, it cannot be stressed enough that the Lagrangian of (4.1) describes a quantum field theory that allows to perform perturbative computations, in principle to any order in the couplings. Thus, the couplings $C_i^{(6)}(\mu)$ do depend on the scale and this dependence is governed by renormalization group equations (RGE) resumming large logarithms $\log(\Lambda/\mu)$. The various operators mix under the RGE. Hence a particular coupling $C_i^{(6)}(M_{ew})$ does in general depend on many $C_j^{(6)}(\Lambda)$.

A first example of the impact of RGE in the context of cLFV processes has been considered in [25] where the branching ratio for $\mu \rightarrow e\gamma$ has been evaluated at leading order in $1/\Lambda^2$, but taking into account one-loop RGE. Doing this, $\text{Br}(\mu \rightarrow e\gamma)$ does not only depend on the coefficient $C_{e\gamma}^{(6)}$ of the dipole operator (expressed in terms of left-handed doublets l , right-handed singlets e and the Higgs doublet Φ)

$$(Q_{e\gamma}^{(6)})_{ij} = (\bar{l}_i \sigma^{\mu\nu} e_j) \Phi F_{\mu\nu} \quad (4.2)$$

with family indices $i, j \in \{1, 2\}$, but also on some four-fermion operators. Limits are always obtained for $C_i^{(6)}/\Lambda^2$. Thus, any statement about probing energy scales of a certain order relies on an assumption about the size of the couplings $C_i^{(6)}$. If, for some weird reason, we expect them

to be $C_i^{(6)} \sim 1$, the energy range probed through the dipole coupling is $\Lambda \gtrsim 10^3$ TeV and the best constrained four-fermion interaction is only slightly weaker. In particular, it should be noted that limits on some four-fermion interactions due to $\mu \rightarrow e\gamma$ can be extremely stringent. Thus, the continuously repeated statement that $\mu \rightarrow e\gamma$ does not constrain contact interactions has to be strongly refuted.

Of course, processes other than $\mu \rightarrow e\gamma$ can be considered as well and this approach allows to relate processes like $\ell_i \rightarrow \ell_j \gamma$ for example to $Z \rightarrow \ell_i \ell_j$. Another interesting option is to consider anomalous magnetic moments or electric dipole moments of leptons in such an approach [26]. In fact, the one-loop anomalous dimensions for all dimension 6 operators of SMEFT have been computed [27, 28]. This allows for the evaluation of the leading logarithms $\log(\Lambda/M_{ew})$ associated with effects of dimension 6 operators for all observables at the EW scale.

5. Effective theory below the electroweak scale

The formalism described in the previous section allows to relate the SMEFT Wilson coefficients at the high scale, $C_i^{(6)}(\Lambda)$, to observables at the EW scale, resumming $\log(\Lambda/M_{ew})$. For processes at the LHC, this is precisely what is needed. However, the processes we are concerned with here take place at an even lower scale. Thus, the appropriate EFT is not SMEFT, but LEFT, an EFT that contains only light fermions, gluons and photons. Furthermore, there is no $SU_L(2)$ symmetry any longer. Thus the higher-dimensional operators of LEFT, \mathcal{Q}_i are not expressed in terms of $SU_L(2)$ doublets l any longer but in terms of left- and right-handed singlet fermion fields, e_L and e_R . Looking at four-fermion interactions, this disentangles neutrino interactions from the corresponding charged lepton interactions. SMEFT four-fermion operators are split into LEFT four-fermion operators like e.g.

$$(Q_{le})_{pqrs} \equiv (\bar{l}_p \gamma^\mu l_q)(\bar{e}_r \gamma_\mu e_s) \xrightarrow{p,q,r=1,s=2} \begin{aligned} \mathcal{Q}_{ee}^{VLR} &= (\bar{e}_L \gamma^\mu e_L)(\bar{e}_R \gamma_\mu \mu_R) \\ \mathcal{Q}_{\nu\nu}^{VR} &= (\bar{\nu}_L \gamma^\mu \nu_L)(\bar{e}_R \gamma_\mu \mu_R) \end{aligned} \quad (5.1)$$

If we keep the assumption that NP enters at a scale $\Lambda \gg M_{ew}$ we obtain \mathcal{L}_{LEFT} from \mathcal{L}_{SMEFT} through matching at the EW scale [29], i.e. we can express $\mathcal{C}(M_{ew})$ in terms of $C(M_{ew})$. However, we can even consider the option that NP actually enters at a scale between the tau mass and the EW scale. In this way, the Wilson coefficients of LEFT such as \mathcal{C}_{ee}^{VLR} and $\mathcal{C}_{\nu\nu}^{VR}$ associated with the operators on the r.h.s. of (5.1) are truly independent. The formal expression for the Lagrangian

$$\mathcal{L}_{LEFT} = \mathcal{L}_{QED} + \mathcal{L}_{QCD} + \frac{1}{M_{ew}} \sum_j \mathcal{C}_j^{(5)} \mathcal{Q}_j^{(5)} + \frac{1}{M_{ew}^2} \sum_i \mathcal{C}_i^{(6)} \mathcal{Q}_i^{(6)} + \dots, \quad (5.2)$$

however, is very similar to (4.1).

We can now express the observables at the (very low) physical scale through Wilson coefficients $\mathcal{C}(\{m_\mu, m_\tau\})$ evaluated at this scale. To make connection to NP, we then relate $\mathcal{C}(\{m_\mu, m_\tau\})$ to $\mathcal{C}(M_{ew})$ or any other scale below the EW scale. For the golden channels this programme has been carried out in [30], including all relevant one-loop anomalous dimensions as well as the two-loop contribution into the dipole operator. As in SMEFT, the operators in LEFT mix under RGE. Hence, if expressed in terms of Wilson coefficients at the EW scale, different observables contribute

to the same operators. This should be seen as a complementarity much more than a competition. Assuming a particular experimental search was to see a deviation, other observables are required to get a handle on what the cause is, i.e. which operator(s) are responsible.

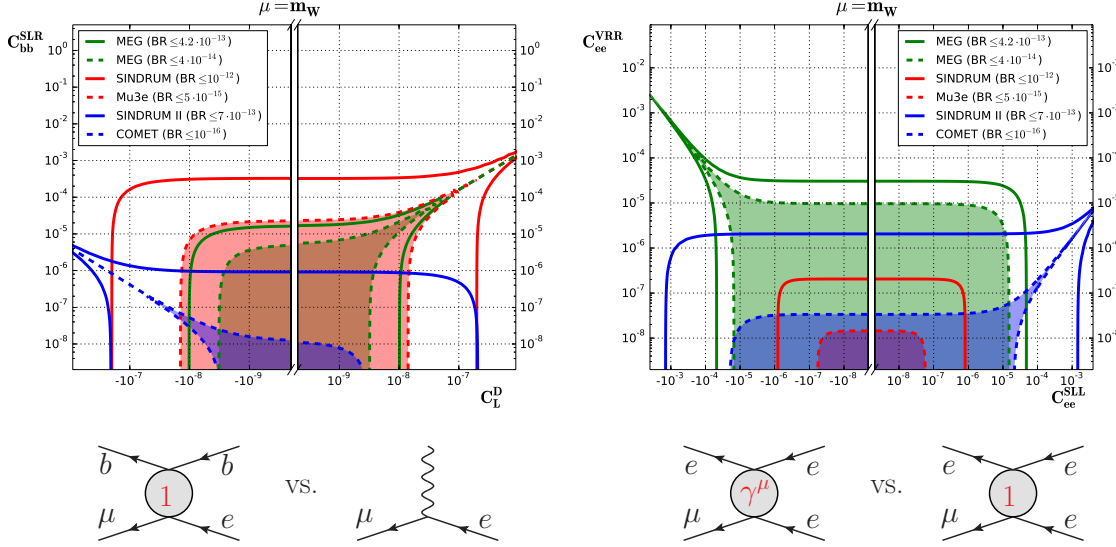


Figure 1:

Comparison of limits obtained from the golden channels on Wilson coefficients $\mathcal{C}(M_{ew})$ of LEFT. Left panel: dipole operator (denoted by C_L^D in the figure) vs. scalar four-fermion operator involving b quarks, C_{bb}^{SLR} ; right panel: vector four-fermion operator C_{ee}^{VRR} vs. scalar four-fermion operator C_{ee}^{SLL} . Figures taken from [30].

In order to illustrate this we consider the impact of current and future limits of the golden channels on various operators. As an example, assume that only the LEFT Wilson coefficients of the dipole operator, denoted by C_L^D , and a scalar four-fermion operator involving b quarks (a contact interaction), denoted by C_{bb}^{SLR} are non-vanishing at the EW scale. The limits obtained are depicted in the left panel of Figure 1. For the dipole operator, the current limit from $\mu \rightarrow 3e$ (red solid line) and muon conversion (blue solid line) are much worse than the corresponding limit from MEG. On the other hand, muon conversion yields a better limit on this particular contact interaction. The improvement due to future measurements are indicated by the dashed lines. Choosing two different operators (right panel of Figure 1) shows a different picture. The decay $\mu \rightarrow 3e$ is the most powerful observable to constrain the scalar contact interaction C_{ee}^{SLL} and the vector contact interaction C_{ee}^{VRR} , followed by muon conversion for the latter. In fact, it is easy to find Wilson coefficients that are most constrained for each of the observables considered. We can even find contact interactions (some tensor interactions, scalar four-fermion interactions involving τ) where $\mu \rightarrow e\gamma$ is the most powerful experiment. Once more, this underlines the statement that $\mu \rightarrow e\gamma$ is very sensitive to contact interactions.

The limit $C_{ee}^{VRR}(M_{ew}) < 2 \times 10^{-7}$ from the Sindrum result $\text{Br}(\mu \rightarrow 3e) < 1 \times 10^{-12}$ (read off from the right panel of Figure 1) can again be interpreted as a NP scale having to be considerably above the EW scale. A naive extrapolation and assuming once more that the NP couplings are

about one, we obtain for the NP scale a limit $\gtrsim 100$ TeV.

The spikes in Figure 1 are due to cancellations between the two operators, indicating that one-at-a-time limits have to be interpreted with caution. We stress that choosing precisely two Wilson coefficients to be non-vanishing is merely due to reasons of presentation. Realistically it should be expected that a particular NP model gives rise to several Wilson coefficients. Performing the RGE also in such a case poses no problems and any model with specific couplings can be tested meaningfully, as soon as the matching coefficients $\mathcal{C}(M_{ew})$ are known.

Finally, we mention that as for SMEFT, all one-loop anomalous dimensions for LEFT are known [31]. Since the dipole operator plays a particularly important role, it is also very useful to consider its two-loop anomalous dimension. Most four-fermion operators only start to mix into the dipole at this level, and including these contributions allows to obtain stringent limits for these contact interactions [30].

6. Conclusions

Charged lepton flavour violating processes provide an opportunity to test the SM to extremely high energy scales of $\sim 100 - 1000$ TeV. Despite having the reputation of being ‘weird’, in many extensions of the SM it is actually more natural to have them than to avoid them. In this short review (see [32] for a more general review) we have concentrated on an EFT treatment of the golden muonic channels, but it goes without saying that tau decays as well as cLFV hadron decays offer additional valuable insight. With the huge experimental progress expected on many cLFV observables in the near future there is every reason to look forward to having another go at the fortress called Standard Model. Whether or not the recent B anomalies survive, the flavour sector can be considered as a weak point of the SM and, hence, should be probed with as much gumption as possible.

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